Accelerated fading recognition for lithium-ion batteries with Nickel-Cobalt-Manganese cathode using quantile regression method

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**HIGHLIGHTS**

- Battery knee point recognition new method using quantile regression is proposed.
- The dynamic boundary determination method for the whole lifetime is developed.
- Recognition result is effective even if the input is disturbed.
- The proposed method has strong reliability and stability at different conditions.

**ARTICLE INFO**

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Accelerated aging
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**ABSTRACT**

The requirement for energy density of lithium-ion batteries becomes more urgent due to the rising demand for driving range of electric vehicles in recent years. Meanwhile, the performance stability of batteries with high energy densities tends to deteriorate, leading to accelerating degradation and safety issues. As a result, it is critical to explore the reasons that yield the sudden degradation and to recognize the degradation knee point of Nickel-Cobalt-Manganese batteries commonly used for electric vehicles. Existing results have disclosed that the lithium deposition of negative electrode dominates the sudden degradation of battery capacity. This paper extracts key parameters that characterize the aging status to facilitate knee point recognition in engineering practice. Furthermore, a novel method that integrates quantile regression and Monte Carlo simulation method to identify the accelerated fading knee point is introduced. The dynamic safety boundary determination method for the whole battery lifetime is proposed to update and monitor the safety zone. It is verified by experiments that the recognition results of capacity degradation knee point appear within 90–95% capacity range at 25 °C, 35 °C and 45 °C conditions, which can provide an early warning before the battery fails. Using the proposed method for recognizing the sudden degradation of capacity, recognition result is effective even if the input is disturbed and has strong reliability and stability under different conditions. It is helpful to promote the sustainable and stable development of the electric vehicles and improve advanced applied energy technologies.

**1. Introduction**

To conserve national energy and reduce emission, developing electric vehicles (EVs) has become a clear trend to deal with energy crisis and increasingly prominent environmental problems \cite{1}. The most concerned quantities for EVs manufacturers and customers are the driving range and service life, which mainly depends on the energy density and remaining life of power batteries. Therefore, the requirement for the energy density of the lithium-ion battery is more rigorous, and its improvement has become the key to promoting the development of EVs \cite{2}.

Nickel-Cobalt-Manganese (NCM) lithium-ion batteries \cite{3} are widely used in EVs due to the higher specific energy and longer cycle life \cite{4} compared with other types of battery. However, NCM batteries with high energy density encounter sudden degradation \cite{5} of battery capacities during usage, which not only greatly reduces the service life and durability of EVs, but also brings serious troubles for users when the EVs is running \cite{6}. In 2017, General Motors Corporation (GM)
suffered a remarkable economy loss from the recall of some Bolt EVs due to the failure of NCM lithium-ion batteries and the reason is that one of the batteries in the battery pack accelerated attenuation, which is also called the capacity “diving”. The voltage of suddenly decaying battery drops rapidly compared with other batteries. Once the battery management system detects that the voltage of any battery in the battery pack is under the limit, it will switch off the power system to avoid over-discharging the battery.

Numerous studies have confirmed that as the lithium-ion battery ages under normal operating conditions, the solid electrolyte interface capacity with the number of cycles [9,10]. Meanwhile, there are some literatures report that the sudden degradation of battery capacity occurs, when the battery suffers from the abuse such as low temperature [11] and high charging cut-off voltage [12], even operates at the normal condition [13,14]. The capacity sudden degradation mechanism of the NCM lithium-ion battery under various operating conditions has been analyzed [15,16]. Zabala et al. [15] evaluated the aging mechanism by in-situ electrochemical measurements and ex-situ destructive physicochemical analysis, confirming that the abrupt decline of capacity is primarily affected by the growth of the SEI layer, resulting in localized lithium plating on the surface of the negative electrode (NE) during extended cycling. Ma et al. [16] systematically explored the effects of electrode material coating, electrolyte additive, upper cutoff voltage, electrolyte concentration, electrode thickness, and graphite type on the sudden degradation of battery capacity, and found that impedance growth is the main cause. It can be concluded that the essential cause of sudden degradation is mainly the lithium deposition of NE, which make the porosity of the electrode to decrease and the SEI layer to grow rapidly. The battery system consists of hundreds or even thousands of lithium-ion batteries connected in series and parallel. Once the sudden degradation occurs, the performance of the battery drops sharply in a short period of time. Furthermore, it is also observed that the batteries begin to expand noticeably since side reactions occur inside the battery, which results in electrolyte decomposition to generate a large amount of gas. This may lead to battery failure and affect the normal operation of the system. In severe cases, the deposited lithium pierces the separator to cause the internal short circuit, and the battery system fires and explodes. This not only causes huge economic losses, but also jeopardizes life safety, greatly restricting the development of energy conversion and conservation technologies.

Real cases of the battery sudden degradation and related mechanism research work have forced us to pay attention to the knee point recognition of sudden degradation for battery capacity. Recognizing the sudden degradation of capacity, it is not only possible to judge the fading trajectory of the battery to play an early warning role, but also to provide guide for replacing the sudden decay battery in time, thereby effectively reducing the safety hazard and improving the performance of the battery pack. It is helpful to promote the sustainable and stable development of the EVs and improve advanced applied energy technologies.

There are few researches on methods for identifying capacity accelerated fading knee point of NCM lithium-ion batteries, but most studies focus on remaining useful life (RUL) prediction and state of health (SOH) estimation. The termination condition of the battery life is generally considered as when the battery capacity declines to 70%-80% of the initial rated capacity or the internal resistance increases to 160%-200% of the initial value. The remaining life can be defined as the length of time from now to the moment when the battery termination condition is reached [17]. The remaining life prediction methods are divided into two categories: model-driven methods and data-driven methods. The fundamental difference between model-based and data-driven methods is whether there is prior knowledge. This prior knowledge may be an empirical model or a physical model that considers the aging mechanism. Model-driven methods have clarified mathematical expression of the battery capacity or internal resistance with respect to the number of cycles before the prediction. Data-driven methods have no well-defined mathematical expression, using a large amount of data to construct an approximate relationship to imitate the real situation.

Implementing the model-driven method has two fold. One relies on the laboratory data under some specific conditions to summarize the evolution law of battery aging, and further establishes empirical models. Another implementation considers the aging mechanism. Ramadesigan et al. [18] and Safari et al. [19] observed chemical reactions and structural changes inside the battery and constructed physicochemical models of battery decay through thermodynamic and kinetic equations. This approach provides a deeper understanding of the decay mechanism of battery capacity, and yields the model having higher prediction accuracy under specific operating conditions than other empirical models. The key of the method is to determine parameters in the model in terms of the measured data when the model structure is determined. A large number of parameter estimation methods such as particle filtering (PF), Kalman filtering (KF), and unscented particle filtering (UPF) have been proposed. Zhang et al. [20] found that the lithium-ion battery capacity declines exponentially and developed a prediction method based on exponential model and PF. Guha et al. [21] combined the double exponential capacity decay model with the fourth-order polynomial internal resistance growth model for the remaining life prediction. Zhang et al. [22] proposed an improved PF algorithm using linear optimization integrated resampling UPF to improve prediction accuracy. In Ref. [23], Markov Chain Monte Carlo (MCMC) methods were used to improve the UPF and establish an empirical capacity decay model. In Ref. [24], Bayesian network theory based model was explored, model parameters were inferred from statistical methods through prior distribution [25,26]. Yang et al. [27] extracted four feature parameters that can well reflect the aging status of batteries as inputs to Gaussian Process Regression (GPR) models. In Ref. [28], the proposed life prediction methods based on multi-hidden nonlinear drift Brownian motion were verified to be more accurate than the PF and Bayesian methods. Although the model-driven methods have a clear expression, it brings unavoidable model prediction error due to uncertainty of model parameters.

Data-driven methods rely on a large amount of existing data rather than a preset model to fit the data with many simple models, finding one or a combination of a set of models that extremely approximate to the real situation. Although the obtained model may have a certain deviation from the real model, in terms of the prediction result, it is sufficiently close to the accurate model within the error tolerance. Data-driven methods can either directly deal with the original data or convert the original data into some features having a certain relationship with predicted values by means of mathematical or signal processing method for machine learning. Li et al. [29] proposed a deep convolutional neural network (DCNN) that uses measured values for learning prediction without known prior distribution. Patil et al. [30] extracted the key feature to construct database from the aging data of lithium-ion battery under different working conditions. Further, an initial estimation was performed to narrow the range of prediction results by using support vector machine (SVM) based classification technique, laying the foundation for accurate life prediction by regression. Wei et al. [31] extracted the time and capacity of the constant voltage (CV) charging process as feature parameters, and established the state space formula based on support vector regression (SVR) that simulates the battery capacity degradation. In Ref. [32], it was found that the capacity of Li(NiCoAl)O2 or LiCoO2 battery showed a downward convex trend with the cycle numbers. In this case, the feature converted from battery capacity via Box-Cox transformation had a clear linear relationship with cycle numbers. Cai et al. [33] processed the raw data based on wavelet transform to build the cross D-Markov machine learning model. In Ref. [34], the charging curve was translated, rotated and scaled based on dynamic space time warping (DSTW), recognizing the
relationship between the judgement curve and reference curve to predict the degradation state. Data-driven methods yield a slightly different model from the real world, but it is sufficient to guide practice. More importantly, data-driven methods can be implemented more easily with the development of computer technology.

All of the aforementioned methods aimed to RUL prediction and SOH estimation, which indicates the remaining life and health status of the battery at the current moment. However, the operating environment of batteries is rather complicated in practical application scenarios. And capacity fading process of batteries is affected by many factors, such as temperature, current, and depth of discharge, which make the accurate prediction of the RUL difficult. Moreover, when a battery starts the accelerated attenuation, the remaining life is less than 20% of the entire life and the consistency difference of the battery pack is great. Under these circumstances, RUL prediction and SOH estimation have estimation errors and uncertainty in the prediction results, it has difficulty in determining whether appearing sudden degradation at current state. In order to avoid the troubles and safety risks mentioned earlier, a method that can quickly and accurately identify the capacity accelerated fading knee point is particularly indispensable.

Based on the investigation of battery degradation mechanisms, this paper extracts the parameters that characterize the state of aging and develops a method integrating quantile regression and Monte Carlo simulation to identify the capacity accelerated fading knee point. The rest of the article will be presented in the following. Section 2 introduces the battery cycle life test matrix. Section 3 depicts the battery degradation mechanism and corresponding characterization parameter extraction. Section 4 presents the principle and implementation of the accelerated fading knee point recognition algorithm. Section 5 demonstrates the identification results and effectiveness analysis of the developed method. Finally, main findings are summarized in Section 6.

2. Battery cycle life test matrix

Cycle life tests under different operating conditions are carried out to study the accelerated fading mechanism and identification method of NCM lithium-ion batteries. The selected battery is a commercial 36Ah NCM lithium-ion battery with the graphite anode. The working voltage ranges from 2.8 V to 4.2 V. Experiments are performed on the platform consisting of a Maccor Battery Testing System, a PC host computer and a thermostat. The test scheme is the constant current-constant voltage (CC-CV) and charge and constant current (CC) discharge. According to the ambient temperature and current rate, the experimental matrix is compartmentalized into four groups, which is recorded in Table 1.

The capacity fading curves under different temperatures are illustrated in Fig. 1. It can be seen that battery capacities under all kinds of cyclic conditions show the accelerated decline stage. The capacities decay slowly and exhibit approximately linear characteristics as the cycle numbers increase at the initial stage. Unexpectedly, the capacity deterioration suddenly accelerates at the end of cycling experiments. When accelerating recession occurs, the sample batteries under the same operating condition have almost identical cycle numbers. For batteries under different temperatures, the cycle numbers show a tremendous difference at the accelerated knee point, which are around 500 cycles at the condition of 25 °C and 1 C charge-1 C discharge (25 °C@1 C–1 C) and 45 °C and 1 C charge-1 C discharge (45 °C@1 C–1 C), 800 cycles at the condition of 35 °C and 1 C charge-1 C discharge (35 °C@1 C–1 C). Furthermore, as the aging accelerates, it is also observed from the experiment that the batteries begin to expand noticeably since side reactions occur inside the battery, which results in electrolyte decomposition to generate gas. The accelerated capacity degradation and drastic appearance change undoubtedly bring great troubles and safety risks to the use of NCM lithium ion batteries, which makes the recession knee point identification extremely urgent.

<table>
<thead>
<tr>
<th>Battery number</th>
<th>Temperature (°C)</th>
<th>Rate (charge-discharge)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1#, 2#</td>
<td>25</td>
<td>1 C-1 C</td>
</tr>
<tr>
<td>3#, 4#</td>
<td>35</td>
<td>1 C-1 C</td>
</tr>
<tr>
<td>5#, 6#</td>
<td>45</td>
<td>1 C-1 C</td>
</tr>
<tr>
<td>7#, 8#</td>
<td>25</td>
<td>0.5 C-1 C</td>
</tr>
</tbody>
</table>

Table 1

Cycle life experimental matrix of NCM lithium-ion batteries under different temperature and rate conditions.

In the interest of identifying the moment when the sudden battery degradation occurs, acquiring the available capacity of the battery is necessary. However, since the battery can hardly be discharged continuously to 0% State-of-Charge (SOC) under practical applications, the true value of the capacity is difficult to obtain and can only be estimated in real time. There is an error in using the real-time capacity estimation method, resulting in inaccurate knee point recognition results. Therefore, finding some characteristic parameters that change drastically after battery sudden degradation to replace the capacity for knee point identification is indispensable. Meanwhile, existing results have disclosed that the lithium deposition on the NE dominates the sudden degradation of battery capacity. For the lithium deposition on the NE, the battery exhibits the abrupt loss of negative active material and available lithium ions. In Ref. [35], a multi-index characterization system revealing the aging state of lithium-ion battery was established by extracting key features from the Increment Capacity (IC) curve at the current rate of 0.05 C. IC curve is derived from the charging curve (Q-V curve). Key features of the IC curve are able to respectively reflect the loss of positive and negative active materials, and available lithium ions, in particular some key features can even be obtained through a partial charging curve, which is more convenient to be implemented in engineering practice. Combined with the capacity sudden degradation mechanism and indicator system of the IC curve, characteristic parameters for the knee point identification are inferred.

For the battery that cycles at 35 °C@1 C–1 C condition, the IC curve at the current rate of 0.05 C is shown in Fig. 2a. The IC curve is obviously composed of three regions shaped like mountains, which are labeled as NEpeak I, NEpeak II and NEpeak III. The voltage points that distinguish different regions are determined by deriving the IC curve. The minimum voltage point that the second derivative of the IC curve is zero is taken as the starting point of NEpeak I. The first local minimum voltage value of the IC curve is regarded as the separation point between NEpeak I and NEpeak II, and the second local minimum voltage value of the IC curve is considered as the separation point between NEpeak II and NEpeak III. The charging cutoff voltage is used as the end point of NEpeak III. Each region has two key features: the area and height of the region. Thus, a total of six features exist: the area and height of NEpeak I, the area and height of NEpeak II, and the area and height of NEpeak III. In our previous papers [35,36], the relationship between IC curve characteristics and battery capacity degradation has been studied and verified by experimental data. It can be roughly maintained that the attenuation of the NEpeak I and NEpeak III region represent the loss of the negative active material and available lithium ions, respectively. And the attenuation of the NEpeak II region simultaneously involves the loss of the two materials. In specific, the area of NEpeak III and the height of NEpeak II reflect the loss of available lithium ions, and the area of NEpeak I and NEpeak II can be used to characterize the loss of the negative active material. Since the amount of available lithium ions and negative active material are suddenly reduced when the battery deterioration is accelerated, the attenuation rate of these four parameters sharply increases. The above IC characteristic parameters are extracted from the charging data at the current of 0.05 C. However, the charging current rate of EVs is much higher than 0.05 C, and the obtained IC curve is somewhat different
from the IC curve at the current of 0.05 C, so that partial IC characteristics become quite inconspicuous. Therefore, it is necessary to expand the charging current to a relatively large rate based on the original IC curve indexing system, so as to determine the specific characteristic parameters for identifying the accelerated knee point.

When the current rate is increased to 1 C, the evolution of the IC curve of the battery that cycles at 35 °C@1 C condition is reported in Fig. 2b. Compared with the IC curve at the current of 0.05 C, the distinct disparity is that the valley point between the NEpeak II and the NEpeak III disappears after the current rate is raised, resulting in the overlap of the two regions. Only by finding a way to separate the two regions, the relevant parameters can be extracted. The IC curve drops sharply after passing the peak of NEpeak II and then enters a platform area gently (NEpeak III). The corresponding entry voltage hardly varies inevitably interfered by the NEpeak III, and the latter also reflects the loss of the negative active material, and the height of NEpeak II is affected by the loss of lithium ions. The demarcation point between the NEpeak II and NEpeak III regions will shift as the battery ages. Affected by the fixed voltage division method, the area of NEpeak II is inevitably interfered by the NEpeak III, and the latter also reflects the loss of lithium ions, so the area of the NEpeak II slightly attenuates. The capacity and three parameters simultaneously began to accelerate the decline, which verifies that the three parameters have the ability to identify the knee point of the battery sudden degradation under different operating conditions. In addition, it can be seen from Fig. 3 that the knee point appears in the 90%-95% capacity range. This is because the experimental data is obtained from the laboratory and only the 25 °C, 35 °C and 45 °C conditions of a type of battery are introduced, the experimental data is obtained from the laboratory and only the different operating conditions, which displays a similar behavior of capacity decay. Moreover, before the sudden degradation, the area of NEpeak I hardly attenuates but the height of NEpeak II presents the slight attenuation. It can be seen that the attenuation mechanism of the battery at this stage is slight lithium ion loss, because the area of NEpeak I is affected by the loss of the negative active material, and the height of NEpeak II is affected by the loss of lithium ions. The demarcation point between the NEpeak II and NEpeak III regions will shift as the battery ages.

Fig. 3 shows the evolution of three IC parameters with cycle numbers under different conditions, which displays a similar behavior of capacity decay. Moreover, before the sudden degradation, the area of NEpeak I hardly attenuates but the height of NEpeak II presents the slight attenuation. It can be seen that the attenuation mechanism of the battery at this stage is slight lithium ion loss, because the area of NEpeak I is affected by the loss of the negative active material, and the height of NEpeak II is affected by the loss of lithium ions. The demarcation point between the NEpeak II and NEpeak III regions will shift as the battery ages.

**Fig. 1.** Capacity retention rate decay curves of NCM lithium-ion batteries under 25 °C@1 C–1 C, 35 °C@1 C–1 C and 45 °C@1 C–1 C conditions (a) Capacity retention rate decay curve at 25 °C@1 C–1 C (b) Capacity retention rate decay curve at 35 °C@1 C–1 C (c) Capacity retention rate decay curve at 45 °C@1 C–1 C.

**Fig. 2.** The IC curve and region division at the charging current rate of 0.05 C and 1 C for the battery cycled under 35 °C@1 C–1 C condition (a) The IC curve and region division of charging at the current of 0.05 C (b) The IC curve and region division of charging at the current of 1 C.
the temperature, charge/discharge rate and depth of discharge are varying under application operating conditions. The reasons of battery sudden degradation are quite complicated resulted from the electrode material, the electrolyte additive, the manufacturing process, and so on. The lab test results can not represent that of the real condition. Therefore, the law of the knee point appears within 90–95% capacity range cannot be directly applied to other conditions. Our approach is designed to provide a general method for identifying the knee point of capacity decline, it is therefore necessary to identify it in real-time. In order to facilitate online capacity degradation identification, it is not desirable to store a large amount of charging data and perform complicated calculations. The height of NEpeak II is an instantaneous variable and can be obtained by finding the maximum value on the IC curve, which is easier to implement than the other two parameters. Ultimately, the height of NEpeak II is applied in the paper to the accelerated degradation identification.

4. Accelerated degradation recognition algorithm

The linear regression model estimates the conditional mean of the response variable given certain values of the predictor variables and the ordinary least squares estimation (OLSE) is the standard estimation method. If the residuals satisfy independence, normality, and homoscedasticity, the OLSE is the unbiased least variance estimate. In practical application scenarios, the measured data is difficult to meet such restricted assumptions. Instead, quantile regression does not require strong assumptions on the error term and can accurately model the effect of the explanatory variables on the range and conditional distribution of the interpreted variable [37]. Regression with various quantiles can get different expressions, which is more comprehensive in portraying the interpreted variables than OLSE [38]. Therefore, for the accelerated fading knee point identification of battery capacity, quantile regression has the potential to perform more reasonably and effectively than the OLSE.

4.1. Quantile regression principle

Suppose the distribution function of the random variable $X$ is:

$$F(x) = P(X \leq x)$$

The $\tau$ quantile can be defined as:

$$Q_\tau(Y|X = x) = \inf \{y \in R: F(y|x) \geq \tau\} (0 < \tau < 1)$$

A random vector $(X, Y)$, where the distribution function of $Y$ given $X = x$ is:

$$F_{Y|X=x}(y|x)$$

The $\tau$ conditional quantile of the conditional random variable $Y|X = x$ is defined as:

$$Q_\tau(Y|X = x) = \inf \{y \in R: F(y|x) \geq \tau\} (0 < \tau < 1)$$

Regression analysis is to minimize the distance between the sample value and the fitted value. Suppose we have a sample sequence: \{$(X_i, Y_i), (i = 1, \ldots, n)$\}

Then the quantile regression is to minimize the sum of the absolute values of the weighted errors, namely:

$$\min \sum_{i=1}^{n} \rho_{\tau}(y_i - \hat{f}(x_i))$$

where $\rho_\tau(u) = u(\tau - 1(u < 0))$ is the loss function and $I(Z)$ is the indicator function on the set $Z$.

When the quantile is 0.5, it is the median regression. Both the loss functions of least squares regression and median regression are symmetric, while the loss function of quantile regression is asymmetric. Actually, it consists of two rays from the origin that are located in the first and second quadrants respectively. Quantile regression is an extension of the least squares method based on the classical conditional mean model. The global model is estimated by multiple quantile functions, and the absolute value of the residual is minimized over asymmetric weights.

If $\hat{y}(x)$ is used to represent the quantile estimator of $y$, then

$$\sum_{i=1}^{n} \rho_\tau(y_i - \alpha)$$

has a minimum value for any value $\alpha$ only when $\alpha = \hat{y}(x)$, where:

$$\sum_{i=1}^{n} \rho_\tau(y_i - \alpha) = -\sum_{i:y_i \leq \alpha} (1 - \tau)(y_i - \alpha) + \sum_{i:y_i > \alpha} \tau(y_i - \alpha)$$

(6)

Assume that the response variable $Y$ is linearly represented by the matrix $X$ consisting of $k$ explanatory variables and the coefficient $\hat{\beta}$ as a linear regression model:

$$y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$

(7)

Then the estimated value of the coefficient of the $\tau$ quantile regression equation is given by:

$$\hat{\beta}(\tau) = \arg \min_{\beta \in R^k} \left( \sum_{i:y_i \leq \beta_0 + \beta_1 x_i} (1 - \tau)\hat{e}(\beta) + \sum_{i:y_i > \beta_0 + \beta_1 x_i} \tau(y_i - \beta_0 - \beta_1 x_i) \right)$$

(8)

$$\hat{\beta}(\tau) = \arg \min_{\beta \in R^k} \left( \sum_{i:y_i \leq \beta_0 + \beta_1 x_i} (1 - \tau)(y_i - \hat{y}(\beta_1)) + \sum_{i:y_i > \beta_0 + \beta_1 x_i} \tau(y_i - \hat{y}(\beta_1)) \right)$$

(9)

where $y_i$ is the actual data, $\hat{e}(\beta)$ represents the residual corresponding to the $\tau$ quantile regression equation. The expression of the $\tau$ quantile regression equation is:

$$\hat{y}(\beta) = \hat{X}\hat{\beta}(\tau)$$

(10)

Once the estimated quantile regression equation is obtained, the linear
relationship between battery capacity and cycling number can be established. More quantile regression equations obtained, more comprehensive understanding of the conditional distribution for explanatory variables. The distribution of explanatory variables is asymmetric when the median regression line is significantly different from the mean regression line. The distribution of response variable is left-biased while the upper quantile regression line is close to the lower quantile regression line, and right-biased otherwise. The coefficient disparity of the regression function is evident and the effect of explanatory variables on the response variable is notably distinct in multiple quantiles.

4.2. Implementation

Lithium-ion batteries experience many kinds of failure modes such as the pole breakage, internal short circuit, battery perforation, deformation, and bulging. Nevertheless, it is difficult to detect the aforementioned failure modes directly since only external parameters including battery terminal voltage, current and temperature can be monitored in real time by employing battery management system (BMS), which does not have a consistent correspondence reflecting the internal failure properties of batteries. Battery failures are usually accompanied by anomalies and reflected in recorded data. This provides a potential for exploring battery safety and fault warning based on the external parameters information of batteries. For example, the battery begins to exhibit bulging when the height of NEpeak II shows a significant knee point. Theoretically, the knee point is the intersection of two straight lines with different slopes, which can be identified according to the sudden change of the slope. Due to the interference of data acquisition and processing error, the slope of the line connected by adjacent cycles is inevitably abrupt, making the method of finding the slope change point difficult to apply. To this end, the paper learns a straight line as the baseline from experimental data and determines the boundary on both sides of the baseline to establish a strip-shaped safety zone. Thus the point beyond the safety zone is considered to be the knee point of the curve. Taking the accelerated fading knee point as the demarcation point, the full life cycle of batteries can be divided into two stages, which are defined as the safe operation stage and the fault operation stage respectively. Battery safety zone and operation stage division diagram is shown in Fig. 4, where “O” represents the knee point in the process of fading. The cycle before the knee point is the safe operation stage, and the subsequent cycle is the fault operation stage. The region within the two boundaries of the baseline is defined as the safety zone, which is determined by the baseline, the distance d-upper from the baseline to the upper boundary, and the distance d-lower from the baseline to the lower boundary. The battery capacity starts accelerating decline when the height of NEpeak II exceeds the safety zone.

After clarifying the definition of the safety zone, the difficulty in identifying the knee point is how to fit the baseline and confirm the boundaries of the strip-shaped safety zone. To resolve the above issue, first of all, the quantile regression algorithm is used to fit the height of the NEpeak II from the decile of 0.5–0.9, and five regression lines are obtained. The regression algorithm should grant higher weight to the previous data since the data of the safe operation stage is linearly degraded. The regression lines with the decile greater than 0.5 quantiles are therefore selected. Therein, a line that minimizes the dispersion of the residual between the estimated value and the true value is chosen as the baseline of the strip-shaped safety zone. Followed by, the values of d-upper and d-lower are determined by performing the Monte Carlo simulation on the residual so that the probability of the height of the NEpeak II being within the safety zone is 95%. Thus the boundaries of the safety zone can be confirmed. Note that the residuals used for the Monte Carlo simulation are determined by their quantile and interquartile range because the height of the NEpeak II is easily interfered by the outliers during the acquisition process. Thus only the data that satisfies the following conditions:

\[ Q_1 - 1.5 \times IQR \leq x \leq Q_3 + 1.5 \times IQR \] (11)

is chosen for the Monte Carlo simulation, where x is the residual between the estimated value and the true value, Q1 and Q3 are the quarter quantile and third-quarter quantile of the residual, respectively, and IQR is the interquartile range of the residual. Residuals outside this range are regarded as outliers based on quantile and interquartile range. It follows that the quantile is more resistant to disturbances since up to 25% of the data can be distributed as far as possible without greatly disturbing the quartile [39]. Therefore, the outliers will not affect the criterion and the corresponding results on identifying outliers are more robust.

Based on the safety boundaries determination, we can find that the probability of the height of NEpeak II exceeding the safety zone is 5%. It is inferred that the probability for four consecutive cycles exceeding the safety zone is less than 0.01%, which can be considered as an event with a very low probability. The last cycle can then be determined as the knee point in the process of capacity fading. In addition, the cycle numbers in the safe operation stage of the battery are difficult to identify due to effects of battery temperature, charge/discharge rate and depth of discharge. It is necessary to continuously update the safety zone with increasing cycle numbers during the whole life of the battery, enhancing the adaptability of the algorithm to different conditions.

The flow chart of the capacity accelerated fading knee point identification of NCM lithium-ion batteries is shown in Fig. 5, which is divided into four steps: (1) feature parameter extraction, (2) safety zone establishment, (3) safety zone update, and (4) accelerated knee point identification. By extending the multi-index aging characterization system to the large-rate charging field and combining with the mechanism of sudden capacity decline, the characteristic parameters for the accelerated knee point identification are extracted. The ribbon safety zone consisting of baseline and bandwidth are finally determined by integrating quantile regression with Monte Carlo simulation. The real-time update of the safety zone can improve the adaptability of the proposed method under various conditions. In a word, the identification of the accelerated recession knee point under different working conditions is implemented.

5. Results and discussion

Fig. 1 shows that the capacity attenuation of the two batteries is consistent at the same temperature. Therefore, one of batteries is selected to perform battery capacity accelerated decay knee point identification under each operating condition based on the proposed method. First of all, the IC curve is derived from the charging curve (Q–V curve) of the selected battery. The height of NEpeak II is extracted from the IC curve to obtain a straight line as the baseline using quantile regression method, and the bandwidths are determined by performing the
Monte Carlo simulation so that the probability of the data being within the safety zone is 95%. After that, if there are four consecutive cycles beyond the safety zone, the last cycle can then be determined as the knee point in the process of capacity fading. In addition, the safety zone is continuously updated with increasing cycle numbers during the whole life of the battery.

The safety zone and the capacity accelerated fading knee point at 25 °C@1 C, 35 °C@1 C and 45 °C@1 C conditions are shown in Fig. 6, and the cycle numbers corresponding to accelerated knee points are 487, 774 and 504, respectively. At present, there is no clear mathematical definition of the knee point. The calculation of the knee point is only by judging whether the change of the slope connected by each adjacent cycles exceeds the threshold, and the threshold is an empirical value and is not fixed. Therefore, there is no reference value for the knee point. It is verified by experiments that the recognition results of capacity degradation knee point using proposed method appear within 90%-95% capacity range, which can provide an early warning before the battery fails. Although the distribution of the height of NEpeak II under the considered three conditions has different characteristics, which is concentrated in Fig. 6a and b, and is seriously disturbed by outliers in Fig. 6a, and while is more scattered in Fig. 6c. From the perspective of results, the proposed method is effective to different data distribution conditions by adaptively adjusting the baseline and computing bandwidth. In more detail, the key procedures of the proposed method are the establishment and update of the safety zone, which determines the effectiveness of the method and require further discussion.

As seen from the establishment of the safety zone in terms of the identification results above, the baseline selection and calculation of the bandwidths \(d_u\) and \(d_l\) are critical factors. Apart from the proposed method, there are two traditional methods that can be adopted as candidates. One method applied the same selection criteria as the proposed method to determine the baseline, as discussed in Section 4. The extreme values of regression residuals were employed to calculate the \(d_u\) and \(d_l\) by Monte Carlo simulation. The height of NEpeak II is not processed and original information is utilized. The other method is to perform a normality test on the residuals between the quantile regression value and true value. The regression line that the residuals pass the normality test is chosen as the baseline and the \("u \pm 3\sigma"\) distance of the residuals is applied to calculate the \(d_u\) and \(d_l\). Once the safety

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**Fig. 5.** The flow chart for the capacity accelerated fading knee point identification of NCM lithium-ion batteries.

**Fig. 6.** The safety zone and the recognition results of capacity accelerated decay knee point using proposed method for NCM lithium-ion batteries under 25 °C@1 C, 35 °C@1 C and 45 °C@1 C conditions (a) The safety zone and the recognition result at 25 °C@1 C (b) The safety zone and the recognition result at 35 °C@1 C (c) The safety zone and the recognition result at 45 °C@1 C.
boundary is successfully established using the three methods, the probability that the height of $N_{\text{peak II}}$ exceeds the safety zone can be clearly defined to facilitate the identification of the acceleration knee point. Their safety zone bandwidths and identification results at 25°C@1C–1C, 35°C@1C–1C and 45°C@1C–1C conditions are comparatively shown in Figs. 7 and 8. For the method of establishing the safe boundary with extreme values, the cycle numbers of accelerated decay knee points are 503, 783 and 510, respectively. Compared with the proposed method, the identification result of the accelerated recession point is delayed, especially for the data distribution with severe interference from outliers, resulting in a broader safety zone. It is highly sensitive to anomalous data for bandwidth calculations, increasing the risk of security incidents. With regard to the method in virtue of the “$u \pm 3\sigma$” principle, the cycle numbers of accelerated recession points at 25°C@1C–1C and 35°C@1C–1C conditions are 494 and 783 respectively, slightly behind the proposed method. Unfortunately, under the condition of 45°C@1C–1C, the data distribution is relatively dispersed, the accelerated decay point could not be identified. Although the “$3\sigma$” principle of normal distribution has the theoretical basis of hypothesis testing, the requirements for real data are too strict to satisfy. Once the residual of the regression line cannot pass the normal test, the “$3\sigma$” standard cannot be used to establish the safety zone for accelerated decay knee point recognition, leading to the failure of method and tremendous safety risk. To sum up, the proposed method can prominently improve the robustness and reliability of the safety zone establishment in comparison with the two traditional methods above.

In addition to the safety zone establishment, another key process affecting the recognition effect is the update of the safety zone. Despite cycle numbers in the safe operation stage are unequal under different operating conditions, the height of $N_{\text{peak II}}$ for all batteries exhibit linearly decaying characteristics, making it unnecessary to continuously update the safety zone after it is initiated. Incipient safety zone can be created with distinct amounts of training data. Fig. 9 shows the results of recognizing the battery capacity accelerated decay knee point with incipient safety zone at 35°C@1C–1C condition. As the amount of training data increases, the knee point cycles identified by the incipient safety zone are postponed, presenting a linear ascending relationship. Under different working conditions, the influence of the training data volume on recognizing result of the accelerated recession knee point is reported in Fig. 10. It can be seen that the accelerated attenuation point fluctuates greatly at 25°C@1C–1C and 35°C@1C–1C conditions, and becomes relatively stable at 45°C@1C–1C condition. This may be because the linearity of the height of $N_{\text{peak II}}$ is discrepant during the safe operation stage. It is concluded that the recognition result of the accelerated recession point may be in advance or delayed when the incipient safety zone is established with various percentages of the total data. They have remarkable influence on the battery usage. The reliability of the battery is improved when the recognition result is in advance, and the battery will not get into the accelerated recession stage, but the economic cost of the battery is inevitably reduced. The battery will be fully utilized if the recognition result is lagging, nevertheless, the safety hazard increases, which may cause serious safety accidents.
battery capacity decay. It is verified by experiments that the recognition results of capacity degradation knee point using proposed method appear within 90%-95% capacity range at 25 °C@1 C–1 C and 45 °C@1 C–1 C conditions, which can provide an early warning before the battery fails. Furthermore, using the proposed method for recognizing the sudden degradation of capacity, recognition result is effective even if the input is disturbed and has strong reliability and stability under different conditions. It is to be regretted that the proposed method is limited to the case where the attenuation of battery capacity at the safe operation stage is approximately linear. For the situation of non-linear attenuation of battery capacity at the safe operation stage, it still needs to be further research.

6. Conclusion

Nickel-Cobalt-Manganese lithium-ion batteries show an accelerated knee point in the capacity degradation process under different conditions. Based on the capacity plummeting mechanism, the paper extends the multi-index aging characterization system to the large-rate charging field and extracts effective characteristic parameters. Furthermore, a novel method for identifying the knee point of capacity decay is explored and the robustness and stability are analyzed. The main contributions are summarized as follows:

1) The essence of capacity plummeting of Nickel-Cobalt-Manganese lithium-ion batteries is the lithium deposition of the negative electrode. The height of NEpeak, reflecting the loss of available lithium ions is strongly correlated characteristic parameter and is also suitable for higher current rate condition which is validated at the current of 1 C.

2) The developed method integrating quantile regression method and Monte Carlo simulation is used to recognize the knee point of the battery capacity decay. It is verified by experiments that the capacity degradation knee point appears within 90%-95% capacity range at 25 °C, 35 °C and 45 °C conditions, which can provide an early warning before the battery fails. Recognition result is effective at different degree of the data dispersion and has adaptability to various conditions of the battery.

3) The establishment and update of the safety zone have significant effect on the recognition results of the proposed method. It is concluded that the bandwidth calculation with the quartile and interquartile range can markedly improve the robustness and reliability of the safety zone establishment compared with two traditional methods. The incipient safety zone is established with various percentages of total data may cause the premature or hysteretic recognition result due to the change of battery degradation speed. The dynamic safety boundary determination method for the whole battery lifetime is therefore proposed to update and monitor the safety zone, making the recognition results exhibit better stability.

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